Estimation of Extraction Pressure EP - 2 December 2020

The main determinants of EP are¹ area A supplied by the capillary, oxygen consumption M and permeability \wp of that area, capillary radius r_c , blood hematocrit Hct, oxygen diffusion coefficient D and red blood cell velocity v_{RBC} . These can be combined in two groups, outside and inside the capillary, and the latter in a standard form, the so-called Peclet number:

(1)
$$Pe = \frac{\Delta z v_{RBC}}{2 D}$$

where Δz is the distance between the erythrocytes, directly related to the hematocrit which is defined as the volume fraction of erythrocytes in the capillary:

(2)
$$V_{RBC} = Hct(V_{RBC} + \pi r_c^2 \Delta z)$$

where V_{RBC} is the volume of a single erythrocyte – the corresponding plasma volume is $\pi r_c^2 \Delta z$. In terms of this Peclet number, a first estimate of EP is:

(3)
$$EP = \frac{MA}{8\pi \wp} \left\{ 1 + \left(\frac{1}{Hct} - 1\right) \frac{c_1}{(c_2 + Pe^2)(c_3 + Hct)} \right\}$$

where c_1 =85, c_2 =130 and c_3 =0.1 for rat heart.

¹ Bos C: Mathematical Modeling of Oxygen Transport from Capillaries to Tissue. Dissertation Thesis, University of Nijmegen.